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CS3252  
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Assignment 9

\* 6.2.2b

PDA to accept all strings with twice as many 0's as 1's:

$$P = (Q, \Sigma, T, \delta, q_0, z_0, f)$$

$$Q = \{q_0, q_f\}$$

$$\Sigma = \{0, 1\}$$

$$T = \{0, H, 1, z_0\} \text{ where } H \text{ means "half"}$$

$$z_0 =$$

$$\delta(q_0, \varepsilon, z_0) = \{(q_0, \varepsilon)\}$$

$$\delta(q_0, 1, z_0) = \{(q_0, 00z_0)\}$$

$$\delta(q_0, 0, z_0) = \{(q_0, Hz_0)\}$$

$$\delta(q_0, 0, H) = \{(q_0, 0)\}$$

$$\delta(q_0, 0, 1) = \{(q_0, H1)\}$$

$$\delta(q_0, 0, 0) = \{(q_0, \varepsilon)\}$$

$$\delta(q_0, 1, 1) = \{(q_0, \varepsilon)\}$$

$$\delta(q_0, 1, c) = \{(q_1, \varepsilon)\}$$

$$\delta(q_1, \varepsilon, 0) = \{(q_0, c)\}$$

$$q_0 = q_0$$

$$z_0 = z_0$$

$$f = \emptyset \quad (\text{acceptance by empty stack})$$

\*6.2.5

b. Execution trace:

$(q_0, abb, z_0)$

↓

$(q_1, bb, AZ_0)$

↓

$(q_1, b, AZ_0)$

↓

$(q_1, \epsilon, z_0)$

↓

$(q_0, \epsilon, z_0)$

↓

$(f, \epsilon)$  acceptance by final state

c.  $(q_0, b^7a^4, z_0)$

↓

$(q_1, b^6a^4, Bz_0)$

each reading of  $b$  with top stack  $B = 1$  move  $B$  on stack

$(q_2, a^4, B^7z_0)$

↓

$(q_3, a^3, B^6z_0)$

↓

$(q_4, a^2, B^5z_0)$

↓

$(q_5, a^2, B^4z_0)$

↓

$(q_6, a^2, B^3z_0)$

$(q_3, a, B^2z_0)$

↓

$(q_2, a, Bz_0)$

↓

$(q_1, \epsilon, z_0)$

After reading  $b^7a^4$  from input, the stack only contains the start symbol,  $z_0$ . If the next epsilon transition is followed, the state of the stack would be  $Az_0$ .

\*6.35

a. PDA:  $(\{q_0, q_1, q_2\}, \{a, b, c\}, \{x, z\}, \delta, q_0, z_0, \phi)$

|  
accept by empty stack

$$\delta(q_0, a, s) = \{(q_0, xxs)\} \text{ where } s \in \Gamma$$

$$\delta(q_0, \epsilon, s) = \{(q_1, s)\} \text{ where } s \in \Gamma$$

$$\delta(q_1, b, s) = \{(q_1, xxz)\} \text{ where } s \in \Gamma$$

$$\delta(q_1, \epsilon, s) = \{(q_2, s)\} \text{ where } s \in \Gamma$$

$$\delta(q_2, c, x) = \{(q_2, \epsilon)\}$$

$$\delta(q_2, \epsilon, z_0) = \{(q_3, \epsilon)\}$$

b. CFG productions:

$$S \rightarrow PC | AQ$$

$$P \rightarrow aaPb | \epsilon$$

$$C \rightarrow CC | \epsilon$$

$$A \rightarrow aA | \epsilon$$

$$Q \rightarrow bQc | \epsilon$$

PDA:  $(\{q^3, \{a, b, c\}^3, \{a, b, c, A, C, P, Q, S\}, \delta, q, s, \phi\})$

$$\delta(q, \epsilon, s) = \{(q, PC), (q, AQ)\} \quad \text{accept by empty stack}$$

$$\delta(q, \epsilon, P) = \{(q, aaPb), (q, \epsilon)\}$$

$$\delta(q, \epsilon, C) = \{(q, CC), (q, \epsilon)\}$$

$$\delta(q, \epsilon, A) = \{(q, aA), (q, \epsilon)\}$$

$$\delta(q, a, a) = \{(q, \epsilon)\}$$

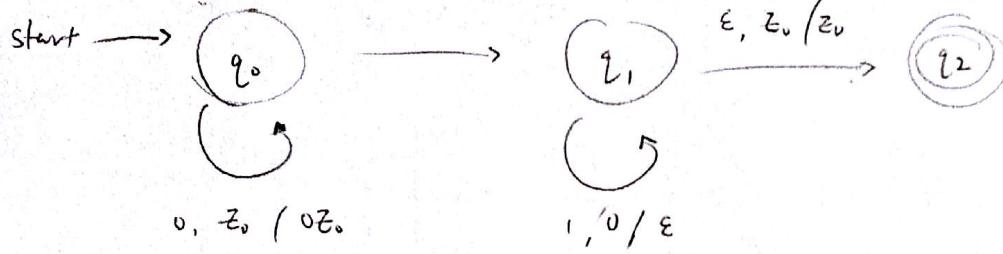
$$\delta(q, b, b) = \{(q, \epsilon)\}$$

$$\delta(q, c, c) = \{(q, \epsilon)\}$$

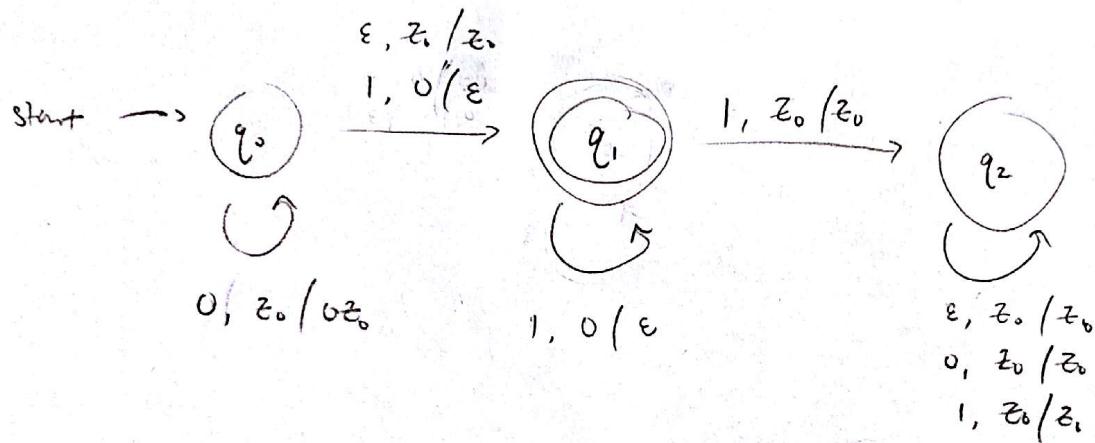
Ex 6.4.2

a.  $\{0^n 1^m \mid n \leq m\}$

$\epsilon, z_0/z_0$   
1, 0,  $\epsilon$



b.  $\{0^n 1^m \mid n \geq m\}$



c.  $\{0^n 1^m 0^n \mid n \text{ and } m \text{ are arbitrary}\}$

